

1 **A powerful framework for integrating eQTL and GWAS**
2 **summary data**

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10 **Short title:** Integrating eQTL and GWAS data

11 **Abstract**

12 Two new gene-based association analysis methods, called *PrediXcan* and *TWAS* for GWAS
13 individual-level and summary data respectively, were recently proposed to integrate GWAS
14 with eQTL data, alleviating two common problems in GWAS by boosting statistical power and
15 facilitating biological interpretation of GWAS discoveries. Based on a novel reformulation of
16 *PrediXcan* and *TWAS*, we propose a more powerful gene-based association test to integrate
17 single set or multiple sets of eQTL data with GWAS individual-level data or summary statis-
18 tics. The proposed test was applied to several GWAS datasets, including two lipid summary
19 association datasets based on $\sim 100,000$ and $\sim 189,000$ samples respectively, and uncovered
20 more known or novel trait-associated genes, showcasing much improved performance of our
21 proposed method. The software implementing the proposed method is freely available as an R
22 package.

23 *Key words:* aSPU test, statistical power, Sum test, transcriptome-wide association study
24 (*TWAS*), weighted association testing.

25 Introduction

26 In spite of many successes, genome-wide association studies (GWAS) face two major challenges.
27 The first is its limited statistical power even with tens to hundreds of thousands of individuals
28 in a typical GWAS or mega-GWAS, thus missing many associated genetic variants, mostly
29 single nucleotide polymorphisms (SNPs), due to the polygenic effects and small effect sizes. The
30 second is that even for those few identified SNPs, since they often do not reside in protein-coding
31 regions, it is difficult to interpret their function and thus biological mechanisms underlying
32 complex traits. A new gene-based association test called *PrediXcan* was recently proposed
33 to integrate GWAS individual-level data with an eQTL dataset, alleviating the above two
34 problems in boosting statistical power of GWAS and facilitating biological interpretation of
35 GWAS discoveries (Gamazon et al 2015). It was extended to GWAS summary association data
36 (Torres et al 2017). A similar approach, called transcriptome-wide association study (TWAS),
37 was proposed by another group for GWAS individual-level and summary data for one or more
38 eQTL datasets (Gusev et al 2016). They are motivated by the key fact that many genetic
39 variants influence complex traits through transcriptional regulation (He et al 2013). Focusing on
40 the genetic component of expression excludes environmental factors influencing gene expression
41 and complex traits, thus can increase statistical power. In addition, compared to standard
42 GWAS, treating genes as analysis units reduces the number and thus burden of multiple tests,
43 again leading to improved power. By applications to common diseases like T2D and complex
44 traits like BMI, lipids and height, the authors have convincingly shown the power of integrating
45 GWAS and eQTL data, gaining biological insights into complex traits. There are more follow-up
46 studies applying TWAS to other diseases. For example, Gusev et al (2017) identified some new
47 genes associated with schizophrenia; interestingly, they also confirmed a previous observation
48 that, contrary to the usual GWAS practice, the nearest gene to a GWAS hit often is not the
49 most likely susceptibility gene, highlighting the critical role of incorporating gene expression to
50 unravel disease mechanisms that may not be achieved by GWAS alone. The current standard

51 and popular view is that PrediXcan and TWAS work because of their predicting or imputing
52 *cis* genetic component of expression for a larger set of individuals in GWAS, facilitating the
53 following expression-trait association testing. Based on this view, some new methods have been
54 proposed to improve over TWAS by addressing some existing weaknesses in gene expression
55 prediction (Bhutani et al 2017; Park et al 2017). In spite of its intuition and usefulness, the
56 current view on PrediXcan and TWAS may not have told the whole story. Here we offer
57 some new insights into PrediXcan and TWAS with a novel reformulation on their underlying
58 association testing. Our key observation is that both PrediXcan and TWAS are based on the
59 same weighted association test; the weights on a set of SNPs in a gene are the *cis*-effects of the
60 SNPs on the gene's expression level (derived from an eQTL dataset). In other words, PrediXcan
61 and TWAS put a higher weight on an SNP (eSNP) that is more strongly associated with the
62 gene's expression level, in agreement with empirical evidence that eSNPs are more likely to
63 be associated with complex traits and diseases (Nicolae et al 2010). This new formulation
64 also points out the connection to existing weighted association analysis (Roeder et al 2006;
65 Ho et al 2014). More importantly, since the same association test in PrediXcan and TWAS
66 suffers from power loss under some common situations, we develop an alternative and more
67 powerful association test with broader applications. Since there is no uniformly most powerful
68 gene-based association test, any single non-adaptive test will lose power in some situations;
69 it is important to develop and utilize adaptive tests to yield consistently high power (Li and
70 Tseng 2011; Lee et al 2012; Pan et al 2014). We propose using such an adaptive and powerful
71 test under a general and rigorous framework of generalized linear models (GLMs), which can
72 accommodate various types of quantitative, categorical and survival phenotypes and can adjust
73 for covariates. It is applicable to both individual-level genotypic, phenotypic data and GWAS
74 summary statistics. It is flexible to incorporate a single or multiple sets of weights derived from
75 eQTL data or other data sources.

76 Methods

77 PrediXcan and TWAS

We briefly review PrediXcan and TWAS for GWAS individual-level data before giving our new formulation. One first builds a prediction model for a gene’s expression level, called “genetically regulated expression (GReX)”, by using the genotypes around the gene based on an eQTL dataset. Next, for a GWAS dataset, one uses the prediction model to predict or “impute” the GReX of the gene using the SNPs around the gene for each subject in a main GWAS dataset. Specifically, for a given gene, suppose that in an eQTL dataset, Y^* and $X^* = (X_1^*, \dots, X_p^*)'$ are the the expression level of of the gene and the p SNP genotype scores (with additive coding) around the gene respectively. A linear model is assumed: $Y^* = \sum_{j=1}^p w_j X_j^* + \epsilon$, where w_j is the *cis*-effect of SNP j on gene expression and ϵ is the noise. Based on the eQTL dataset, one can use a method, e.g. elastic net (Zou and Hastie 2005) or a Bayesian linear mixed model (Zhou et al 2013) as used in PrediXcan and TWAS respectively, to obtain the estimates \hat{w}_j ’s. Now for a given GWAS dataset, for each subject i with the genotype scores $X_i = (X_{i,1}, \dots, X_{i,p})'$ for the gene, the predicted GReX is $\widehat{\text{GReX}}_i = \sum_{j=1}^p \hat{w}_j X_{i,j}$. For a trait Y_i for subject i in the GWAS dataset, one simply applies a suitable GLM

$$g(E(Y_i)) = \beta_0 + \widehat{\text{GReX}}_i \beta_c = \beta_0 + \sum_{j=1}^p \hat{w}_j X_{i,j} \beta_c \quad (1)$$

78 to test for association between the trait and predicted/imputed expression with null hypothesis
 79 $H_0: \beta_c = 0$, where $g()$ is the canonical link function (e.g. the logit and the identity functions
 80 for binary and quantitative traits respectively), and $E(Y_i)$ is the mean of the trait. One of the
 81 asymptotically equivalent Wald, Score and likelihood ratio tests can be used.

82 A novel reformulation and extensions

Here we first point out that PrediXcan and TWAS can be regarded as a special case of general association testing with multiple SNPs in a GLM:

$$g(E(Y_i)) = \beta_0 + \beta' X_i = \beta_0 + \sum_{j=1}^p X_{i,j} \beta_j. \quad (2)$$

83 The goal is to test $H_0 : \beta = (\beta_1, \dots, \beta_p)' = 0$. It can be verified that both PrediXcan and
 84 TWAS are a weighted Sum test in the above general model (Pan 2009) with weights \hat{w}_j on each
 85 SNP j ; that is, PrediXcan and TWAS conduct the Sum test on H_0 with the genotype scores
 86 $X_{i,j}$ replaced by the weighted genotype scores $\hat{w}_j X_{i,j}$ in GLM (2). This new interpretation
 87 and formulation will facilitate our gaining insights into PrediXcan and TWAS, including their
 88 possible limitations, thus motivating some modifications for improvement. It offers a direct and
 89 intuitive justification for PrediXcan and TWAS: the two methods perform well due to their
 90 over-weighting on expression-associated SNPs (eSNPs), as supported by empirical evidence
 91 that eSNPs are more likely to be associated with complex traits and disease (Nicolae et al
 92 2010). Obviously, it also suggests their extensions to other endophenotypes, and to incorporate
 93 prior knowledge and other data sources related to the GWAS trait of interest, such as previous
 94 linkage scans (Roeder et al 2006) and imaging endophenotypes (Xu et al 2017), though we
 95 do not pursue it here. More importantly, since the Sum test can be derived under the over-
 96 simplifying working assumption of $\beta_1 = \beta_2 = \dots = \beta_p = \beta_c$ in (1) and (2) (i.e. all weighted
 97 SNPs have an equal effect size and the same effect direction, which is in general incorrect), we
 98 can see possible limitations of the Sum test and thus of PrediXcan and TWAS. As discussed in
 99 Pan (2009), Pan et al (2014) and others (Wu et al 2011), the Sum test may lose power if the
 100 effect directions of the (weighted) SNPs are different, or the effect sizes are sparse (i.e. with
 101 many 0s). Accordingly, one may apply other tests, e.g. the sum of squared score (SSU) test
 102 that is equivalent to a variance-component score test as used in kernel machine regression (also

103 known as SKAT in rare variant analysis) with a linear kernel and a nonparametric MANOVA
 104 (also called genomic distance-based regression) with the Euclidean distance metric (Wessel and
 105 Schork 2006), which may yield higher power under many situations (Pan 2011; Schaid 2010a,
 106 2010b).

107 **New method: aSPU**

A class of the so-called sum of powered score (SPU) tests cover both the Sum and SSU tests as special cases. Specifically, we denote the unweighted and weighted score vectors for β in (1) as

$$U^* = (U_1^*, \dots, U_p^*)' = \sum_{i=1}^n X_i'(Y_i - \hat{\mu}_i^0), \quad U = (U_1, \dots, U_p)' = WU^* = \sum_{i=1}^n WX_i'(Y_i - \hat{\mu}_i^0),$$

where $\hat{\mu}_i^0$ is the fitted mean of Y_i under H_0 (with $\beta = 0$) in (1), and $W = \text{Diag}(\hat{w}_1, \dots, \hat{w}_p)$ are the weights of the SNPs derived from an eQTL dataset. The effects of the weights can be regarded as replacing the unweighted genotype scores $X_{i,j}$ by the weighted genotype scores $\hat{w}_j X_{i,j}$ in GLM (2). The Sum (i.e. PrediXcan and TWAS) and SSU tests based on the weighted genotypes are:

$$T_{\text{Sum}} = \sum_{j=1}^p U_j, \quad T_{\text{SSU}} = U^T U = \sum_{j=1}^p U_j^2.$$

More generally, for an integer $\gamma \geq 1$, an $\text{SPU}(\gamma)$ test is defined as

$$T_{\text{SPU}(\gamma)} = \sum_{j=1}^p U_j^\gamma.$$

108 It is clear $\text{SPU}(1)=\text{Sum}$ and $\text{SPU}(2)=\text{SSU}$. Furthermore, for an even integer $\gamma \rightarrow \infty$, we have
 109 $T_{\text{SPU}(\gamma)} \propto \left(\sum_{j=1}^p |U_j|^\gamma\right)^{1/\gamma} \rightarrow \max_j |U_j| = T_{\text{SPU}(\infty)}$. The $\text{SPU}(\infty)$ is closely related to the
 110 UminP test (but ignoring possibly varying variances of U_j 's); often they performed similarly
 111 (Pan 2009).

112 Since there is no uniformly most powerful test, for a given situation, any non-adaptive test

113 may or may not be powerful. By using various values of γ , we yield a class of SPU tests, one of
 114 which is expected to be more powerful in any given situation. For example, the Sum=SPU(1)
 115 test treats each SNP equally *a priori*, yielding high power if all the SNPs are associated with
 116 the trait with similar effect sizes and the same association direction. On the other hand, when
 117 only a smaller subset of SNPs are associated with the trait, or their association directions are
 118 different, the SSU=SPU(2) test is often more powerful. As γ increases, SPU(γ) relies more on
 119 the SNPs that are more strongly associated with the trait, and is thus more powerful for more
 120 sparse association signals (i.e. fewer associated SNPs). In the end, as γ approaches ∞ (as an
 121 even integer), it only considers the most significant SNP.

Since the optimal value of γ is unknown and data-dependent, we propose using an **adaptive SPU (aSPU)** test to data-adaptively approximate the most powerful SPU test among a set of versatile SPU(γ) tests with various values of γ , thus maintaining high power in a wide range of scenarios. Empirically we have found that using $\Gamma = \{1, 2, 3, \dots, 6, \infty\}$ often performs well and thus adopt it; the aSPU test is defined as

$$T_{aSPU} = \min_{\gamma \in \Gamma} P_{SPU(\gamma)}, \quad (3)$$

122 where $P_{SPU(\gamma)}$ is the p-value of the SPU(γ) test.

123 P-value calculations: Although asymptotic p-values for the SPU(1)=Sum and SPU(2)=SSU
 124 tests can be calculated (Pan 2009) (with possible small-sample adjustments (Lee et al 2012;
 125 Chen et al 2015; Wang 2016)), in general, we can use *one layer of Monte Carlo simulations*
 126 to estimate the p-values for all the SPU and aSPU tests *simultaneously* (Pan et al 2014).
 127 Specifically, we simulate null score vectors $U^{(b)} \sim N(0, V)$ for $b = 1, \dots, B$, from its asymptotic
 128 null distribution, a multivariate normal with mean 0 and covariance matrix V ; there is a
 129 closed form solution for V (Pan et al 2014). Then the null statistics $T_{SPU(\gamma)}^{(b)}$ are calculated
 130 from the null score vectors $U^{*(b)}$ for $b = 1, \dots, B$, and the p-value of the SPU(γ) test is
 131 $P_{SPU(\gamma)} = [\sum_{b=1}^B I(|T_{SPU(\gamma)}^{(b)}| \geq |T_{SPU(\gamma)}|) + 1]/(B + 1)$. Then the p-value for the aSPU test

132 is calculated as $P_{\text{aSPU}} = [\sum_{b=1}^B I(T_{\text{aSPU}}^{(b)} \leq T_{\text{aSPU}}) + 1]/(B + 1)$ with $T_{\text{aSPU}}^{(b)} = \min_{\gamma \in \Gamma} p_{\gamma}^{(b)}$ and
 133 $p_{\gamma}^{(b_1)} = [\sum_{b \neq b_1} I(|T_{\text{SPU}(\gamma)}^{(b)}| \geq |T_{\text{SPU}(\gamma)}^{(b_1)}|) + 1]/B$.

134 Association testing with summary statistics

135 One practical way to increase the sample size is to form large consortia, aiming for meta
 136 analysis of multiple GWAS, for which often only summary statistics for single SNP-single
 137 trait associations, rather than individual-level genotypic and phenotypic data, are available
 138 (and practically feasible for many cohorts with possibly different study designs). Hence it
 139 is extremely useful to develop methods like TWAS that are applicable to GWAS summary
 140 statistics as well as to GWAS individual-level data. The aSPU test is easily extended to GWAS
 141 summary statistics without individual-level data. Suppose that $Z_j = \hat{\beta}_j/\text{SE}_j$ is the Z-statistic
 142 for association between the GWAS trait and SNP j , where $\hat{\beta}_j$ is the estimated (marginal and
 143 signed) association effect and SE_j is its standard error. We just need to simply redefine $U = WZ$
 144 with $Z = (Z_1, Z_2, \dots, Z_p)'$, then proceed as before. We use a reference sample (e.g. the 1000
 145 Genome Project data) to estimate linkage disequilibrium (LD) among the SNPs and thus the
 146 correlation matrix for Z and U (Kwak and Pan 2016; Gusev et al 2016).

147 Association testing with multiple sets of weights

Now we extend the aSPU test to the case with multiple sets of eQTL datasets, or more generally,
 multiple sets of weights. This is important because of the existence of multiple eQTL datasets
 measured from different populations or different tissues; it is in general unclear which one is
 most suitable. After applications with each eQTL dataset separately, it may gain statistical
 power and biological insights to combine the results across multiple eQTL datasets. Suppose
 we have K sets of weights, $W^{(k)} = \text{Diag}(w_1^{(k)}, \dots, w_p^{(k)})$ for $k = 1, 2, \dots, K$, each estimated
 from a separate eQTL dataset. To avoid the results depending on the varying scales of the
 sets of weights, we first standardize the weights to have $\sum_{j=1}^p |w_j^{(k)}| = 1$ for each k . Based on

the score vector U^* (with individual-level data) or Z-statistics Z (with GWAS summary data) and the weights $W^{(k)}$, we define $U^{(k)} = W^{(k)}U^*$ or $U^{(k)} = W^{(k)}Z$ accordingly. As before, for a fixed γ , we first apply SPU(γ) to $U^{(k)} = (U_1^{(k)}, \dots, U_p^{(k)})'$, yielding its test statistic $T_{SPU(\gamma;k)} = \sum_{j=1}^p (U_j^{(k)})^\gamma$ and p-value $P_{SPU(\gamma;k)}$. We then Z-transform each p-value to a Z-statistic $z^*(\gamma; k) = 1 - \Phi^{-1}(P_{SPU(\gamma;k)}/2)$, where $\Phi(\cdot)$ is the CDF of a standard normal distribution. To recover the sign of each statistic, for an odd γ , we have $z(\gamma; k) = \text{sign}(T_{SPU(\gamma;k)})z^*(\gamma; k)$; for an even γ or $\gamma = \infty$, we use $z(\gamma; k) = \text{sign}(T_{SPU(1;k)})z^*(\gamma; k)$. We combine the K sets of weights through combining the K statistics $z(\gamma) = (z(\gamma; 1), \dots, z(\gamma; K))'$ to form an omnibus SPU(γ) test:

$$\text{SPU}(\gamma)\text{-O} = [z(\gamma) - \mu_0(\gamma)]'V^{-1}(\gamma)[z(\gamma) - \mu_0(\gamma)],$$

where $\mu_0(\gamma)$ and $V^{-1}(\gamma)$ are the sample mean vector and covariance matrix of $z(\gamma)$ under H_0 , which can be calculated along with other p-values inside the single layer of simulations. Then, as usual, we combine the omnibus SPU(γ)-O tests into an omnibus aSPU test:

$$T_{\text{aSPU-O}} = \min_{\gamma \in \Gamma} P_{\text{SPU}(\gamma)\text{-O}},$$

148 where $P_{\text{SPU}(\gamma)\text{-O}}$ is the p-value of SPU(γ)-O. As before, the p-values of all the SPU(γ)-O and
 149 aSPU-O can be calculated in a single layer of Monte Carlo simulations.

150 The omnibus test is not sensitive to weight standardization. For example, scaling by
 151 $\sum_j (w_j^\kappa)^{(1/\kappa)}$ yielded similar results in our experiments.

152 It is easy to verify that SPU(1)-O is equivalent to the omnibus TWAS, denoted TWAS-O.
 153 Again, by combining SPU(1)-O and other SPU(γ)-O tests, we obtain the adaptive and omnibus
 154 aSPU-O test that may be more powerful across a wide range of scenarios.

155 **Data availability**

156 The WTCCC data can be found at <https://www.wtccc.org.uk>. The original 2010 lipid
157 GWAS summary data can be downloaded at [http://csg.sph.umich.edu/abecasis/public/
158 lipids2010/](http://csg.sph.umich.edu/abecasis/public/lipids2010/), while the original 2013 lipid GWAS summary data at [http://csg.sph.umich.
159 edu/abecasis/public/lipids2013/](http://csg.sph.umich.edu/abecasis/public/lipids2013/); the two pre-processed datasets that we used are down-
160 loadable from https://figshare.com/articles/Lipid_2010_summary_data/5373370 and https://figshare.com/articles/Lipid_2013_summary_data/5373382. The LD reference data and
162 eQTL-based weights can be obtained from <http://gusevlab.org/projects/fusion/> and
163 <https://github.com/hakyimlab/PrediXcan>. The related computer scripts and examples
164 can be found at <https://github.com/ChongWu-Biostat/TWAS>, and the online manual about
165 how to use our proposed methods can be also found at www.wuchong.org/TWAS.html or
166 <https://github.com/ChongWu-Biostat/TWAS>.

167 **Results**

168 **Application to the WTCCC data**

169 We first applied the aSPU test and PrediXcan to the WTCCC individual-level data with
170 the weights downloaded from the PrediXcan database, demonstrating the equivalence of the
171 SPU(1) test and PrediXcan, and more importantly, that the aSPU test could identify more
172 associated genes than PrediXcan in many cases. Specifically, first, following the same proce-
173 dure of quality control (Burton et al 2007), we lifted the annotation of the WTCCC geno-
174 type data from hg18 to hg19 via the UCSC browser ([http://genome.ucsc.edu/cgi-bin/
175 hgLiftOver](http://genome.ucsc.edu/cgi-bin/hgLiftOver)); second, we imputed the genotype data via the Michigan Imputation Server
176 with the following specifications: 1000G Phase 1 v3 as the reference panel, SHAPEIT as
177 the phasing algorithm and EUR (European) as the target population. After imputation, the
178 variants with a minor allele frequency (MAF) > 0.05 , the HWE exact test P -value > 0.05

179 and $R^2 > 0.8$ were kept. As Gamazon et al (2015), we kept only the HapMap Phase 2
 180 subset of SNPs. We considered 7 traits/diseases: bipolar disorder (BD), coronary artery
 181 disease (CAD), inflammatory bowel disease (CD), rheumatoid arthritis (RA), hypertension
 182 (HT), type 1 diabetes (T1D) and type 2 diabetes (T2D). The weights based on the DGN
 183 whole blood expression were downloaded from the PrediXcan database (<https://app.box.com/s/gujt4m6njqqc9tu0oqgtjvtz9860w>). There were 8917 genes whose expression levels
 185 could be predicted by elastic net with a cross-validated $R^2 > 0.01$; we thus tested on these
 186 8917 genes with a conservative Bonferroni adjustment with a genome-wide significance level at
 187 $0.05/9000 = 5.56 \times 10^{-6}$.

188 As most of the genes were not expected to be significantly associated with a trait, we used a
 189 step-up procedure to increase the number of simulations when calculating the p-values of aSPU
 190 and aSPU-O in the subsequent data analysis. We started with a relatively small $B = 10^3$, and
 191 re-ran the tests with $B = 10^4$ for the genes with p-values $< 5 \times 10^{-3}$ (but stopped otherwise);
 192 we repeated this process by increasing B to 10 times of its previous value for the genes with
 193 p-values $< 5/B$ up to $B = 1 \times 10^7$; finally, to be more accurate for a p-value around the
 194 significance cut-off, we re-ran the tests on the genes with p-values between 10^{-5} and 10^{-6} with
 195 $B = 1 \times 10^8$.

196 Here are the main results. First, as shown in Supplementary Figure 1, as expected, PrediX-
 197 can gave essentially the same results (i.e. p-values) as those of the SPU(1) test for each of the
 198 seven traits. Hence, we confirmed and would treat the SPU(1) test to be equivalent to PrediX-
 199 can. Second, as shown in Supplementary Figure 2, the aSPU test identified more significant
 200 genes than the SPU(1) test (or equivalently, PrediXcan) for traits CD, BD and T1D (i.e. (10,
 201 3, 38) versus (8, 2, 29)), while it was the opposite for HT (i.e. 0 versus 1), and they were tied
 202 (with (1, 4, 0)) for CAD, RA and T2D; note the large difference for T1D, which was statistically
 203 significant with an exact p-value=0.0039 by McNemar’s test (Fagerland et al 2013) (while other
 204 differences were not). Table 1 lists the significant genes identified by the aSPU test but not by
 205 the SPU(1) test (and PrediXcan) at the genome-wide significance level; some of the significant

206 genes were confirmed in later studies. In total, we identified 15 new genes, five out of which
207 have been reported by other studies. For CD, we identified 4 new genes, all of which contained
208 some genome-wide significant SNPs identified by other studies, constituting a highly significant
209 validation of our discoveries. Specifically, genes IRGM, P4HA2, PTGER4, and RBM22 contain
210 significant SNPs rs11741861 ($p = 2 \times 10^{-19}$, de Lange et al 2017), rs2188962 ($p = 6 \times 10^{-36}$, de
211 Lange et al 2017), rs11742580 ($p = 7 \times 10^{-36}$, Franke et al 2010), and rs11741861 ($p = 2 \times 10^{-19}$,
212 de Lange et al 2017), respectively. Importantly, gene IRGM is related to CD pathogenesis with
213 the involvement in the process of autophagy (Liu et al 2015). However, our newly identified
214 genes JAKMIP1 and PDK1, associated with BD and CAD respectively, have not yet been
215 reported elsewhere. For T1D, we identified 9 new genes, of which one contains some genome-
216 wide significant SNPs as reported by another study (Plagnol et al 2011). In summary, these
217 15 significant genes identified by the aSPU test would have been missed by PrediXcan, some
218 of which have been confirmed by other studies while the remaining ones are to be validated in
219 the future.

220 **Application to the lipid GWAS summary data**

221 We next applied our new methods and TWAS to a 2010 lipid GWAS summary dataset ($\sim 100,000$
222 samples, Teslovich et al 2010), while using its follow-up with a larger sample size ($\sim 189,000$)
223 for partial validation. To facilitate comparison, we used the three sets of weights and the 1000
224 Genomes Project data as the reference sample, all downloaded from the TWAS database (<http://gusevlab.org/projects/fusion/#reference-functional-data>) (on *Jan 11th, 2017*). The
225 three sets of weights were based on three eQTL datasets: microarray gene expression data of
226 peripheral blood from 1,245 unrelated subjects from the Netherlands Twin Registry (NTR)
227 (Wright et al 2014), microarray expression data of blood from 1,264 subjects from the Young
228 Finns Study (YFS), and RNA-seq measured in adipose tissue from 563 individuals from the
229 Metabolic Syndrome in Men study (METSIM); for each pair of gene-eQTL dataset, we used the
230

Table 1. Significant genes identified by the aSPU test, but not by the SPU(1) test (or PrediXcan) at the genome-wide significance threshold of 5.56×10^{-6} . The validated gene-trait associations appeared in the following references: [1] Franke et al (2010); [2] Kenny et al (2012); [3] de Lange et al (2017); [4] Plagnol et al (2011).

Trait	Gene	Chr.	SNPs in		SPU(1)	SPU(2)	Reported Valid. ref
			#SNPs	aSPU			
CD	IRGM	5	34	5.0E-07	1.7E-04	3.8E-08	CD [1]
	P4HA2	5	7	2.5E-06	1.7E-01	8.4E-07	CD [2]
	PTGER4	5	22	1.1E-06	1.0E-05	2.6E-07	CD [1]
	RBM22	5	15	7.0E-07	1.4E-02	5.5E-06	CD [3]
BD	JAKMIP1	4	21	1.0E-07	1.8E-05	3.2E-09	-
CAD	PDK1	2	33	5.5E-06	5.8E-03	2.7E-05	-
T1D	ALDH2	12	19	1.0E-07	6.6E-05	1.1E-07	-
	BCL2L15	1	21	1.0E-07	5.1E-04	2.1E-06	T1D [4]
	HFE*	6	61	7.0E-07	5.8E-01	5.7E-08	-
	MPHOSPH10	2	20	6.0E-07	1.2E-01	1.4E-07	-
	PGBD1*	6	33	1.0E-07	3.0E-04	2.4E-09	-
	PRSS16*	6	32	1.5E-06	6.3E-05	2.0E-07	-
	TMEM116	12	23	2.0E-06	5.0E-04	6.9E-07	-
	ZNF193*	6	64	1.0E-07	2.3E-02	5.0E-11	-
ZSCAN12*	6	14	4.0E-07	8.1E-06	2.5E-06	-	

* The genes fall in the HLA region.

231 set of the optimal weights estimated by TWAS. For each trait, there were 1264, 3555 and 2295
 232 significant cis-heritable genes with weights drawn from the NTR, YFS and METSIM eQTL
 233 datasets respectively, resulting in a total of 7114 genes being tested; when combining across
 234 three sets of weights, there were 1223 genes being tested by the omnibus TWAS and thus con-
 235 sidered as the candidate genes by any omnibus test. Thus, we used a conservative Bonferroni
 236 adjustment with $0.05/8500 = 5.88 \times 10^{-6}$ as the genome-wide significance level. The GWAS
 237 Z-scores were imputed for any missing SNPs using the IMPG algorithm (Pasaniuc et al 2014).

238 The new test identified more associations

239 We numerically confirmed the equivalence between the SPU(1) test and TWAS (Supplementary
 240 Figure 3). Hence, we used the results of the SPU(1) test to represent those of TWAS in the
 241 following. More importantly, the aSPU test could identify a larger number of significant genes

Table 2. The numbers of the significant genes identified by analyzing the 2010 lipid data for each single set of the weights and the combined one (i.e. with the omnibus aSPU and TWAS tests). The numbers a/b/c in each cell indicate the numbers of (a) the significant genes; (b) the significant genes that covered a genome-wide significant SNPs in the 2010 lipid data; (c) the significant genes that covered a genome-wide significant SNPs in the 2013 lipid data.

Trait	Test	NTR	YFS	METSIM	Combined
HDL	aSPU	19/16/17	29/27/29	22/19/22	21/17/17
	TWAS	16/14/15	25/22/24	19/15/19	20/16/17
LDL	aSPU	15/15/15	19/18/18	17/16/17	14/13/13
	TWAS	8/7/8	10/9/9	7/7/7	7/7/7
TG	aSPU	17/16/17	33/30/32	15/14/14	20/19/19
	TWAS	9/9/9	17/16/17	8/7/7	12/11/11
TC	aSPU	26/25/26	28/26/27	28/28/28	20/20/20
	TWAS	15/14/15	18/16/17	15/14/15	14/13/13

242 than TWAS in every case across the four traits (HDL, LDL, TC and TG) and three sets
 243 of weights (NTR, YFS and METSIM); the same conclusion holds for the omnibus aSPU and
 244 omnibus TWAS tests (Table 2). As a partial validation, a high proportion of the identified genes
 245 covered at least one genome-wide significant SNP in the 2010 ($\sim 100,000$ samples) or the larger
 246 2013 data ($\sim 189,000$ samples, Global Lipids Genetics Consortium 2013). In Supplementary
 247 Tables 1-7, we list the significant genes identified by aSPU and TWAS based on analyzing the
 248 2010 lipid data, including novel ones not overlapping with any known risk loci covering any
 249 significant SNPs ($P < 5 \times 10^{-8}$) in the 2010 data (Supplementary Tables 1-2) or in the larger
 250 2013 lipid GWAS dataset (Supplementary Tables 3).

251 Compared to TWAS, the aSPU test can still maintain high power if many of the SNPs in a
 252 gene are not associated with a trait. For example, based on the 2010 data, for trait HDL and
 253 gene DR1 with the YFS-based weights, among the 17 SNPs with non-zero weights, there were
 254 only one SNP with a p-value less than 5×10^{-7} (but larger than the genome-wide significance
 255 level 5×10^{-8}), resulting in a non-significant p-value ($= 1.4 \times 10^{-4}$) by TWAS, or equivalently
 256 by SPU(1). Since an SPU(γ) test with a larger $\gamma > 1$ relied more on the SNPs with the smaller
 257 p-values (i.e. more strongly associated with the trait), it yielded a more significant p-value with
 258 a larger γ : the SPU(2) and SPU(5) tests gave p-value $= 2.9 \times 10^{-6}$ and 3.5×10^{-6} respectively,

Table 3. The numbers of the significant genes identified by analyzing the 2013 lipid data for each single set of the weights and the combined one (i.e. with the omnibus aSPU and TWAS tests). The numbers a/b/c in each cell indicate the numbers of (a) the significant genes; (b) the significant genes that covered a genome-wide significant SNPs in the 2010 lipid data; (c) the significant genes that covered a genome-wide significant SNPs in the 2013 lipid data.

Trait	Test	NTR	YFS	METSIM	Combined
HDL	aSPU	21/18/21	52/39/48	33/24/32	31/21/29
	TWAS	21/17/20	35/26/33	24/17/23	26/16/24
LDL	aSPU	24/23/24	40/34/37	27/24/26	20/17/18
	TWAS	16/14/16	28/23/25	16/14/15	17/15/16
TG	aSPU	21/19/21	43/37/42	26/20/25	23/21/23
	TWAS	15/13/15	27/22/25	15/12/15	16/15/16
TC	aSPU	36/27/35	70/52/66	42/36/42	37/32/36
	TWAS	25/18/24	38/28/35	26/21/26	25/20/23

259 leading to the significant p-value = 2.3×10^{-6} of aSPU in the end. Furthermore, based on
 260 the 2013 data, several SNPs in the locus were genome-wide significant, and both aSPU and
 261 TWAS confirmed the significance of gene DR1. Two locusZoom plots for the locus based on
 262 the 2010 and 2013 data are shown in Figure 1. Another similar example is with the 2010 data
 263 for trait TG and gene NEIL2 with the NTR-based weights: although all the five weighted score
 264 elements for the SNPs were negative, their absolute values varied from 0.07 to 2.89, leading
 265 to the p-values $< 5 \times 10^{-6}$ for any SPU(γ) with $\gamma > 1$, more significant than the p-value =
 266 8.8×10^{-6} of SPU(1).

267 An SPU(γ) test with an even γ could be more powerful than SPU(1) with varying SNP
 268 association directions. In the 2010 data, for trait LDL and gene NTN5 with the METSIM-based
 269 weights, among the 450 weighted score elements of the individual SNPs, 43% were positive while
 270 the remaining 57% were negative, leading to a much more significant p-value of SPU(2) over
 271 that of SPU(1): 8.2×10^{-8} versus 4.9×10^{-5} .

272 Generally, as expected from statistical theory and as shown in Supplementary Figures 4-5,
 273 since the SPU(1) test (i.e. TWAS) might not be powerful for a given gene, the aSPU test could
 274 gain statistical power through other more powerful SPU tests like SPU(2).

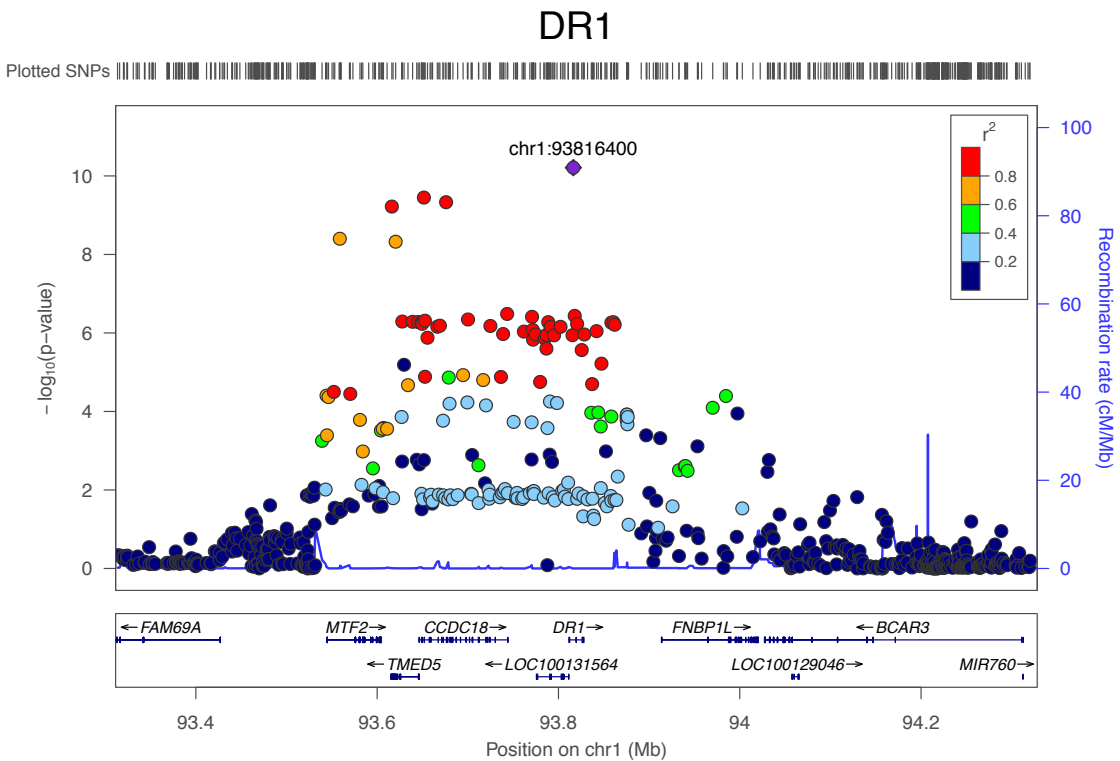
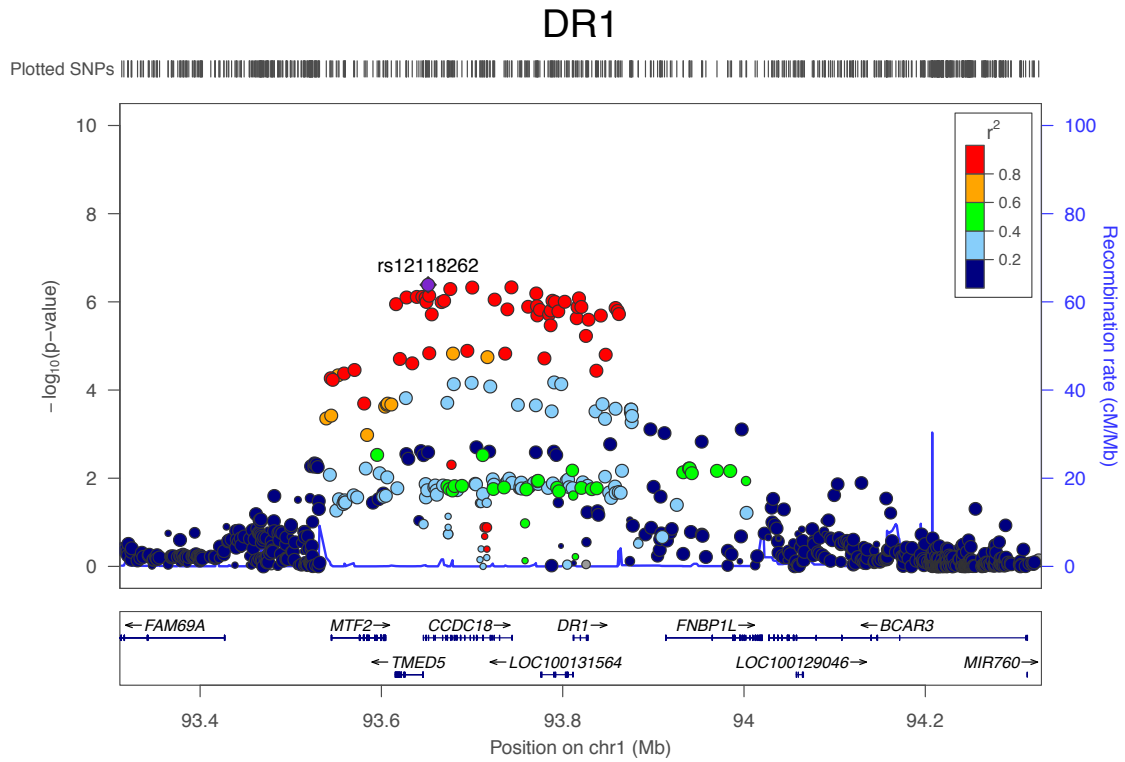


Figure 1. LocusZoom plots of SNP-HDL associations at the locus around gene DR1 based on the 2010 lipid data (top) and 2013 data (bottom).

275 **The new test identified novel associations**

276 Finally, we applied the aSPU and TWAS (and their omnibus versions) to the larger 2013 lipid
277 dataset (Global Lipids Genetics Consortium 2013), listing the numbers of the significant genes
278 identified by each method in Table 3. Again the aSPU test identified a much larger number
279 of significant associations. The Manhattan plots for the pooled results of aSPU for each set of
280 the weights and of aSPU-O combining the three sets of the weights for each trait are shown
281 in Figures 2-3; a comparison between aSPU/aSPU-O versus TWAS/TWAS-O for trait LDL
282 is shown in Supplementary Figures 6-7. In total, aSPU and TWAS identified 17 and 14 new
283 associations not overlapping with known risk loci respectively; among the 6 new associations
284 uniquely identified by aSPU test, gene PFAS was reported to be associated with LDL in a later
285 meta-analysis (Below et al 2016). The new associations identified by aSPU or/and TWAS are
286 listed in Table 4, while all other ones are in Supplementary Tables 8-11. It is noteworthy that
287 in Table 4, with the p-values close to the significance cut-off, the aSPU test barely missed the
288 three significant genes uniquely identified by the SPU(1) test (i.e. TWAS); in contrast, the
289 SPU(1) test gave the much larger p-values for several significant genes uniquely identified by
290 aSPU.

291 **Simulations**

292 It was shown previously that the aSPU test could control its type I error rate effectively in
293 the context of unweighted association testing (Pan et al 2014), which is expected to hold in
294 the current context. Nevertheless, we conducted a simulation study to confirm it. We used
295 the individual-level (imputed) genotypic data of the WTCCC control and T2D samples with
296 a combined sample size of $n = 4862$. We randomly generated a binary trait with an equal
297 probability 0.5 (of being in either category) for each subject, and calculated a summary Z
298 statistic for each SNP. We then applied the aSPU test along with the asymptotic SPU(1)
299 and SPU(2) tests to the individual-level data with the same PrediXcan-constructed weights

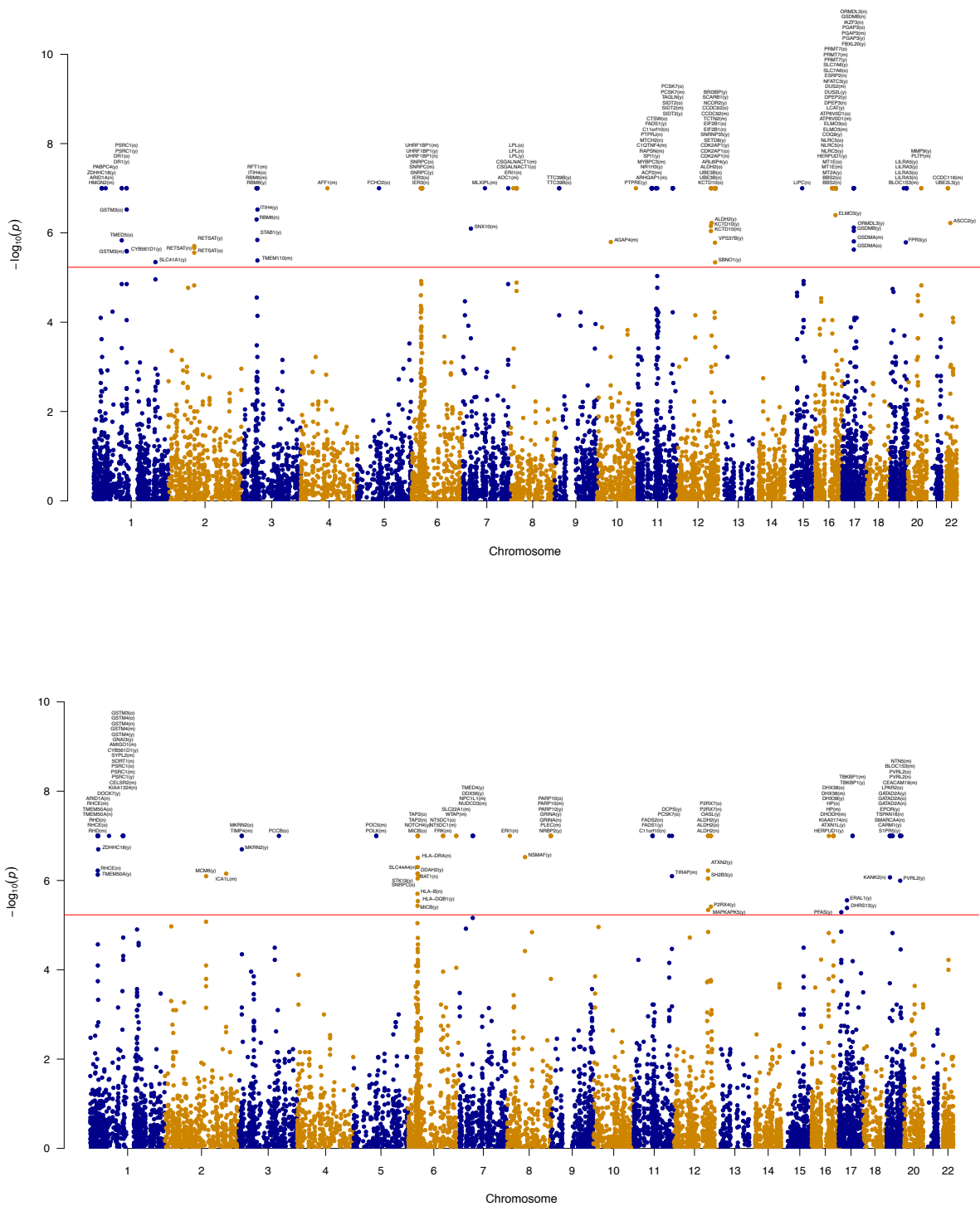


Figure 2. Manhattan plots for the pooled results of aSPU and aSPU-O for traits HDL (top) and LDL (bottom) based on the 2013 lipid data. The letters “(n)”, “(y)”, “(m)” and “(o)” following a gene’s name indicate the result of aSPU based on the NTR, YFS and METSIM weights and that of aSPU-O respectively.

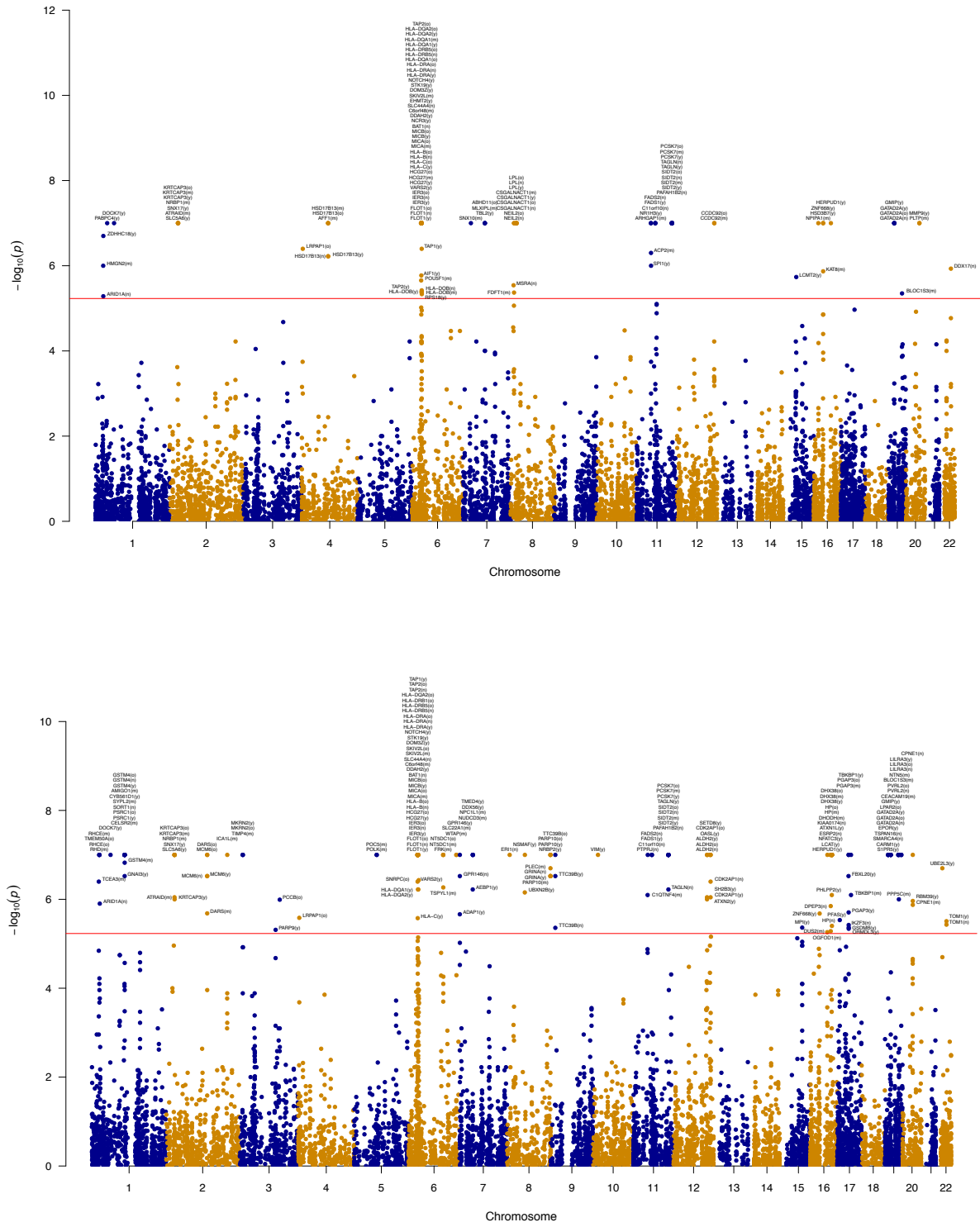


Figure 3. Manhattan plots for the pooled results of aSPU and aSPU-O for traits TG (top) and TC (bottom) based on the 2013 lipid data.

Table 4. Significant gene-trait associations identified by aSPU or/and TWAS with no known risk loci within 500kb. The column “Sig.test” indicates the corresponding association was detected by aSPU or SPU(1) or both.

Trait	Weight	Gene	Chr.	Locus start	Locus end	aSPU	SPU(1)	SPU(2)	Sig.test
HDL	YFS	SLC41A1	1	205758221	205782876	4.5E-06	7.9E-04	2.2E-04	aSPU
HDL	YFS	ASCC2	22	30184597	30234271	6.0E-07	9.7E-04	6.2E-06	aSPU
LDL	YFS	PFAS	17	8150936	8173809	5.1E-06	4.2E-03	1.1E-06	aSPU
TG	METSIM	ARHGAP1	11	46698630	46722165	1.0E-07	3.8E-04	1.2E-08	aSPU
TC	YFS	ZNF668	16	31072164	31085641	2.1E-06	3.7E-05	1.4E-05	aSPU
TC	YFS	PFAS	17	8150936	8173809	2.9E-06	5.4E-03	1.8E-06	aSPU
LDL	YFS	HSPA6	1	161494036	161496681	2.8E-05	4.6E-06	3.2E-02	SPU(1)
TG	YFS	PACS1	11	65837834	66012218	8.2E-06	5.7E-06	1.2E-06	SPU(1)
TC	YFS	ADCY3	2	25042038	25142708	1.1E-05	4.1E-06	2.5E-02	SPU(1)
HDL	NTR	RETSAT	2	85569078	85581848	2.2E-06	1.3E-06	2.3E-06	Both
HDL	YFS	RETSAT	2	85569211	85581743	2.0E-06	2.3E-06	1.5E-06	Both
HDL	YFS	PTPRE	10	129705325	129884119	1.0E-07	3.7E-08	1.4E-01	Both
HDL	METSIM	SNX10	7	26331541	26413949	8.0E-07	5.6E-07	8.7E-07	Both
LDL	YFS	ERAL1	17	27181956	27188085	2.8E-06	1.7E-06	2.2E-06	Both
LDL	YFS	DHRS13	17	27224799	27230089	4.1E-06	2.2E-06	2.4E-06	Both
LDL	METSIM	ICA1L	2	203640690	203736708	7.0E-07	2.1E-07	5.9E-07	Both
TG	YFS	LCMT2	15	43619974	43622803	1.8E-06	1.6E-06	3.2E-06	Both
TC	NTR	ARID1A	1	27022521	27109023	1.2E-06	9.7E-07	1.4E-06	Both
TC	YFS	PARP9	3	122246771	122283424	4.9E-06	2.4E-06	3.7E-06	Both
TC	YFS	MPI	15	75182346	75191798	4.3E-06	6.1E-07	6.8E-07	Both

300 based on the DGN whole blood gene expression data; in addition, we also applied the tests
301 to the summary Z-statistics with the TWAS-constructed weights based on the NTR, YFS and
302 METSIM gene expression data respectively; finally, we applied the omnibus aSPU-O test to
303 the summary statistics to combine results across the three sets of NTR, YFS and METSIM
304 weights. Similar to that in the real data analysis, we used a step-up procedure to adaptively
305 determine the number of simulations when calculating the p-values of aSPU and aSPU-O. We
306 started with a relatively small $B = 10^3$; we re-ran the tests with $B = 10^4$ for the genes with
307 p-values $< 5 \times 10^{-3}$, but stopped otherwise; we repeated this process by increasing B to 10
308 times of its previous value for the genes with p-values $< 5/B$ up to $B = 1 \times 10^7$. As shown
309 in the Q-Q plots in Supplementary Figure 8, in each case each test controlled the type I error
310 rate satisfactorily.

311 Discussion

312 We note that the algorithm in PrediXcan and TWAS (for quantitative GWAS traits) is similar
313 to two-stage least squares (2SLS) with the SNPs as instrumental variables, which is related
314 to the Mendelian Randomization (MR) approach of Zhu et al (2016). However, since only
315 *cis*-eQTLs are considered in the above approaches (while *trans*-eQTLs are ignored), the used
316 SNPs may be weak instrumental variables and the assumptions underlying MR are likely to be
317 violated. Hence we have so far avoided a causal interpretation of detected associations.

318 In summary, we have developed a powerful adaptive test (aSPU) to integrate GWAS and
319 eQTL data. We have demonstrated its improved power over the existing methods; in fact,
320 the same association test underlying the two existing methods, PrediXcan and TWAS, can
321 be regarded as a special case of our proposed test, explaining why our proposed test may
322 have improved power. Importantly, our new formulation of PrediXcan and TWAS in the
323 general framework of weighted multi-SNP association testing suggests other possible extensions,
324 e.g. applications not only to other informative endophenotypes (Xu et al 2017), but also to

325 incorporate other sources of information like SNP functional annotation, previous linkage scans
326 (Roeder et al 2006) and multiple phenotypes (Kim et al 2015; Zhu et al 2015), which may be
327 worth to be investigated in the future.

328 The proposed statistical tests are implemented in R package `aSPU2`, which along with some
329 example R code is publicly available at www.wuchong.org/TWAS.html.

330 Supplemental information

331 Supplemental Data include 8 Supplementary Figures and 11 Supplementary Tables.

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